

Green's Theorem

Group Members:

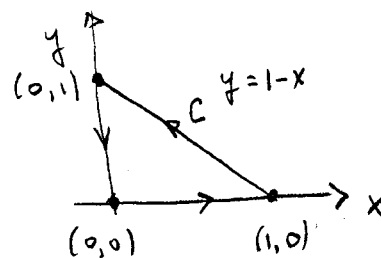
1. _____
2. _____
3. _____
4. _____

Work together as a team to solve the following problems.

1. Evaluate the following line integral by using Green's Theorem (Hint: integrate over the inside of the region).

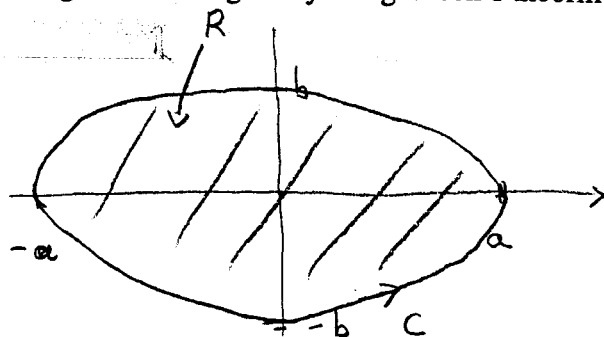
$$\int_C x^4 dx + xy dy = \int_C P dx + Q dy = \int_C \vec{F} \cdot d\vec{r} = \int_C \vec{F} \cdot \vec{r}'(t) dt$$

a) What do $P(x,y)$, $Q(x,y)$, $\vec{F}(x,y)$ equal?



b)
$$= \iint_R (\text{curl } \vec{F})_z dA = \iint_R \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) dA.$$
 Set up and evaluate.

2. Evaluate the following integral over a region by using Green's theorem to evaluate it on the boundary of the region.



$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

$$\iint_R 1 \, dA = \frac{1}{2} \oint_C x \, dy - y \, dx = \oint_C \vec{F} \cdot d\vec{r}$$

a) Show by Green's Thm That $\oint_C (-y, x) \cdot d\vec{r} = \iint_R 1 \, dA = \text{Area}(R)$

$$P(x, y) =$$

$$\frac{\partial P}{\partial y} =$$

$$\left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right)$$

$$Q(x, y) =$$

$$\frac{\partial Q}{\partial x} =$$

=

b) Evaluate the line integral $\oint_C (-y/2, x/2) \cdot r'(t) \, dt$

Parametrization:

$$x(t) =$$

$$y(t) =$$

$$t \in [,]$$